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In collaborazione



INAF-OAA

Titolo:
**Metrologia ottica con i comb per
l'astronomia**

Relatore:
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Sede:
Osservatorio Astrofisico di Arcetri
Largo Enrico Fermi, 5 Firenze



- Astronomical motivations
- The ideal calibration source of wide bandwidth astronomical spectrographs
- The optical frequency comb (OFC) as calibration source
- Interferential optical filtering of an OFC
- Design and development of a filtering system
 - Filtering with Fabry-Perot cavities with dielectric coated mirrors
 - Filtering with Fabry-Perot cavities with metallic coated mirror
- Conclusions and perspectives with different approaches



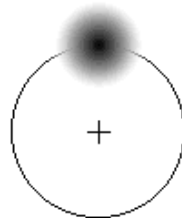
Astronomical motivations

- Search for extra-solar planets via indirect methods: Radial Velocity Method

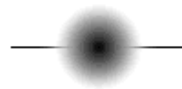
$$v_r \propto \left(\frac{M_1}{P} \right)^{1/3} \frac{q}{(1 - q)^{2/3}} \sin i$$

P : orbital period
 M_1, M_2 : mass of star, planet
 $q = M_2 / M_1$
 i : inclination of orbital axis

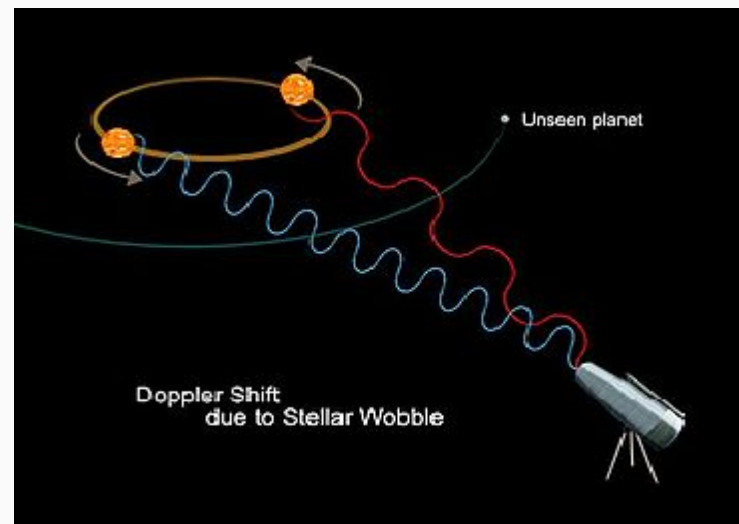
orbit of the star
around the
center of mass



projected
orbit



observed
Doppler shift





Astronomical motivations

- Search for extra-solar planets: measuring velocity wobble with precisions ranging from cm/s to m/s
- Determination of the universe's expansion history: measuring the evolution of the cosmological red-shift of distant objects with a precision of $1 \text{ cm s}^{-1} \text{ yr}^{-1}$
- Measurement of the variability of fundamental constants: comparing laboratory and distant objects spectra



Possible by using a very large number of absorption lines of the astronomical object and statistical analysis by cross-correlation technique



High resolution astronomical spectrometers, operating in a wide spectral region and **calibrated with high precision and in real-time**



Astronomical motivations

• Search for extra-solar planets:

Sun-like start \longrightarrow **Jupiter:** $v_r \sim 10$ m/s
Earth: $v_r \sim 10$ cm/s

Earth-like planet around M-type dwarf stars:

- easier to detect;
- most common stars (80% in our galaxy).

\longrightarrow $v_r \sim 1$ m/s

The **GIANO spectrograph at TNG**: Near-IR (0.95 – 2.5 μm) echelle spectrograph

Resolving power $\rightarrow R = 50000$ $\Delta\lambda_{max} = 2 \times 10^{-5} \lambda \rightarrow \Delta f_{max} = 4$ GHz (at 1.5 μm).

Precision $\rightarrow \frac{\Delta\lambda}{\lambda} = \frac{v_r}{c} \sim 3 \times 10^{-9}$



The ideal calibration source

The ideal calibration spectrum would comprise lines which:

- (i) have known wavelengths ;
- (ii) are individually unresolved;
- (iii) are resolved from each other;
- (iv) have uniform spacing;
- (v) cover the whole range of operation;
- (vi) have nearly uniform intensity;
- (vii) are stable over long-time scales;
- (viii) don't reduce S/N of observed object.

moreover:

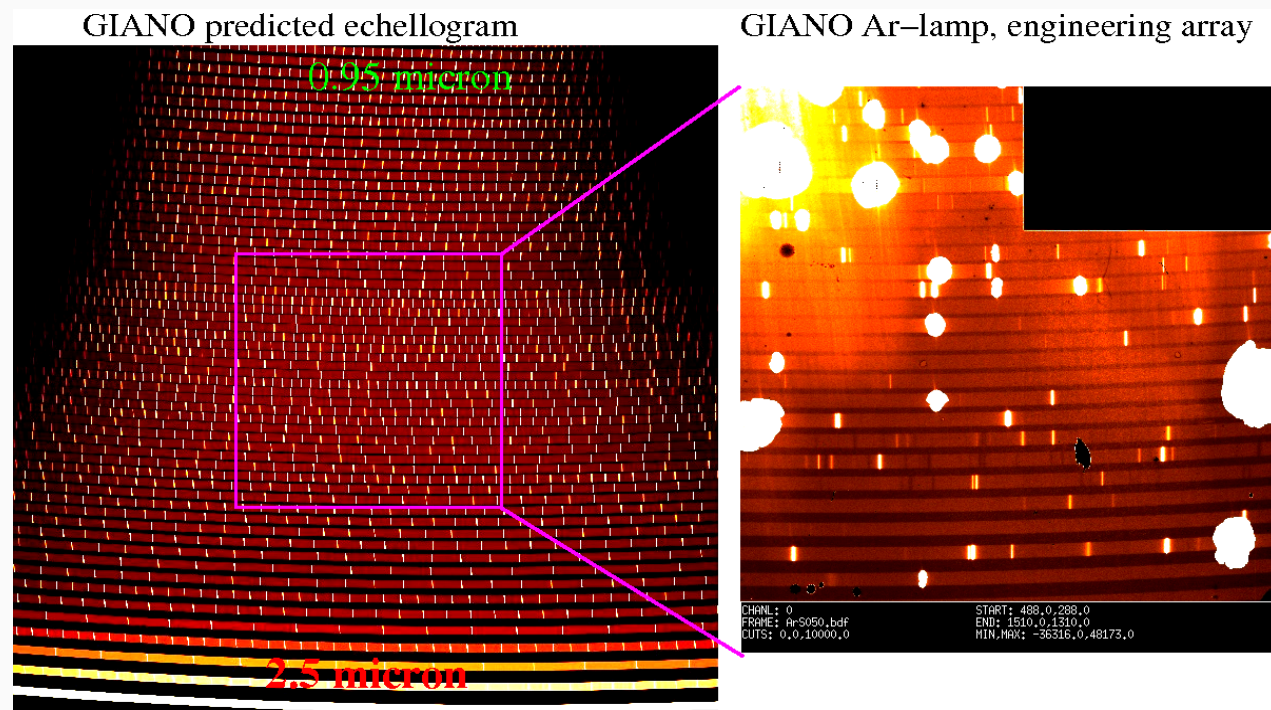
- (ix) exchangeable (2 independent sources produce the same spectrum);
- (x) easy to use (nearly turn-key);
- (xi) reasonably low costing.



The ideal calibration source

Limitations of the current standard calibration source in the near-IR: Th-Ar discharge lamp

comparison with
the ideal
calibration
spectrum:



The nearly-ideal calibration source has been identified as
the Optical Frequency Comb

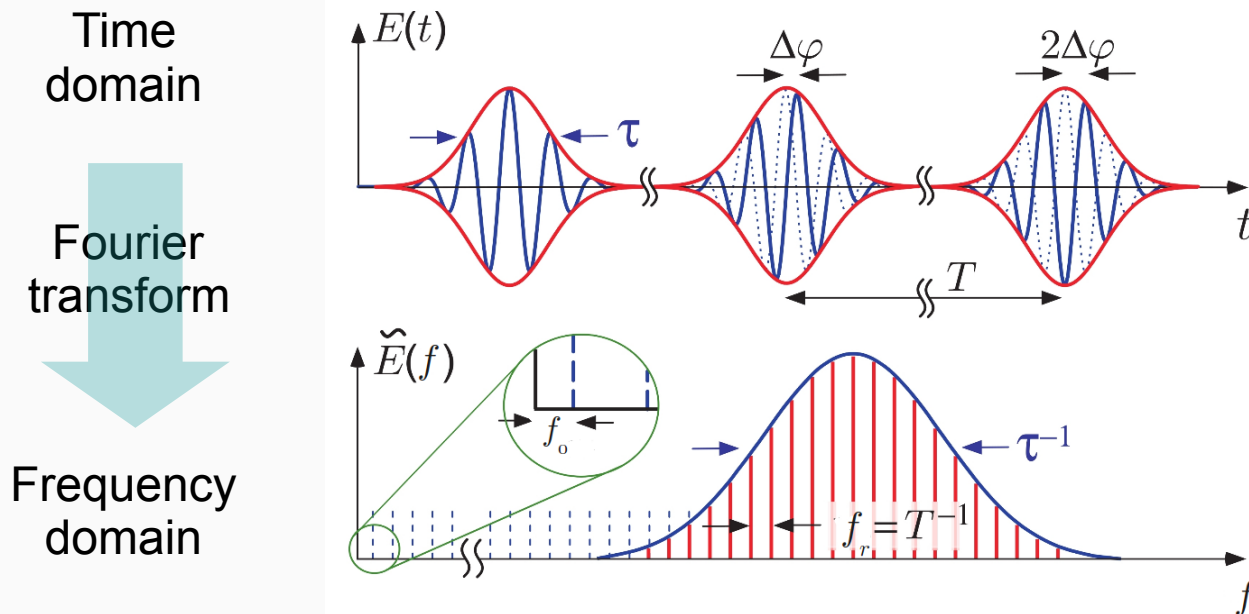
(Murphy et al. 2007, MNRAS 380, 839; Osterman et al. 2007, SPIE 6693, 66931G1)



The optical frequency comb (OFC)

Principles of operation

Mode-locked pulsed laser: store a single pulse (\sim tens fs) and maintain it on a repetitive path, emitting a copy of the pulse after each round-trip, resulting in an train of pulses



$$f_n = n f_r + f_0$$

n integer and f_0, f_r radio-frequencies
controllable against atomic clocks
($< 250\text{MHz}$ for commercial near-IR combs)

$$\frac{\Delta f_n}{f_n} \leq 10^{-12}$$

$$\Delta f \propto \tau^{-1} \Rightarrow \text{tens nm}$$

Easily broadened to one octave in the near-IR by non-linear effects in optical fibers



The optical frequency comb (OFC)

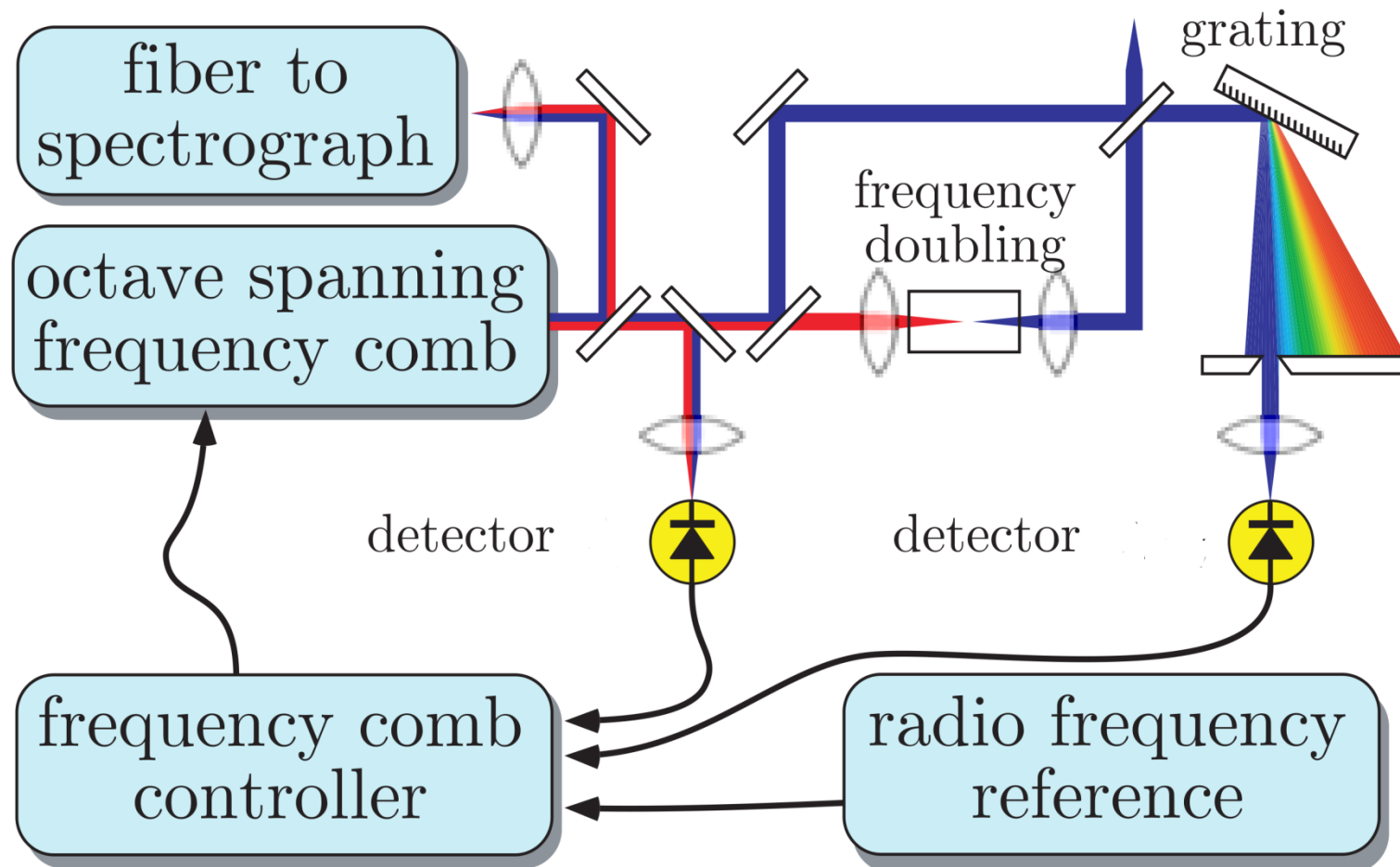
A quasi-ideal calibration spectrum:

- (i) have known wavelengths ;
- (ii) are individually unresolved;
- (iii) are resolved from each other;
- (iv) have uniform spacing;
- (v) cover the whole range of operation;
- (vi) have nearly uniform intensity;
- (vii) are stable over long-time scales;
- (viii) don't reduce S/N of observed object.
- (ix) exchangeable (2 independent sources produce the same spectrum);
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The optical frequency comb (OFC)

The Astro-comb set-up





The optical frequency comb (OFC)

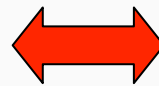
Not-resolved comb spacing problem

FC1500 Er-doped fiber OFC
(MenloSystems GmbH):

$f_r = 100\text{-}250$ MHz

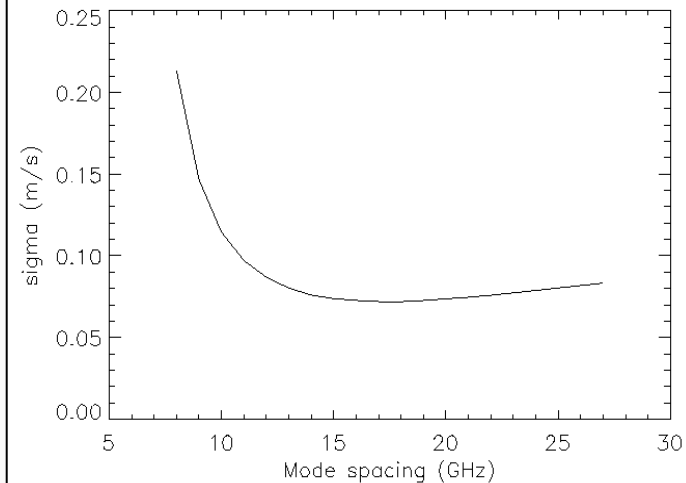


Spectral coverage: 1 – 2 μm



GIANO:

optimum line spacing:
16 GHz



Possible solution: **Interferential optical filtering**



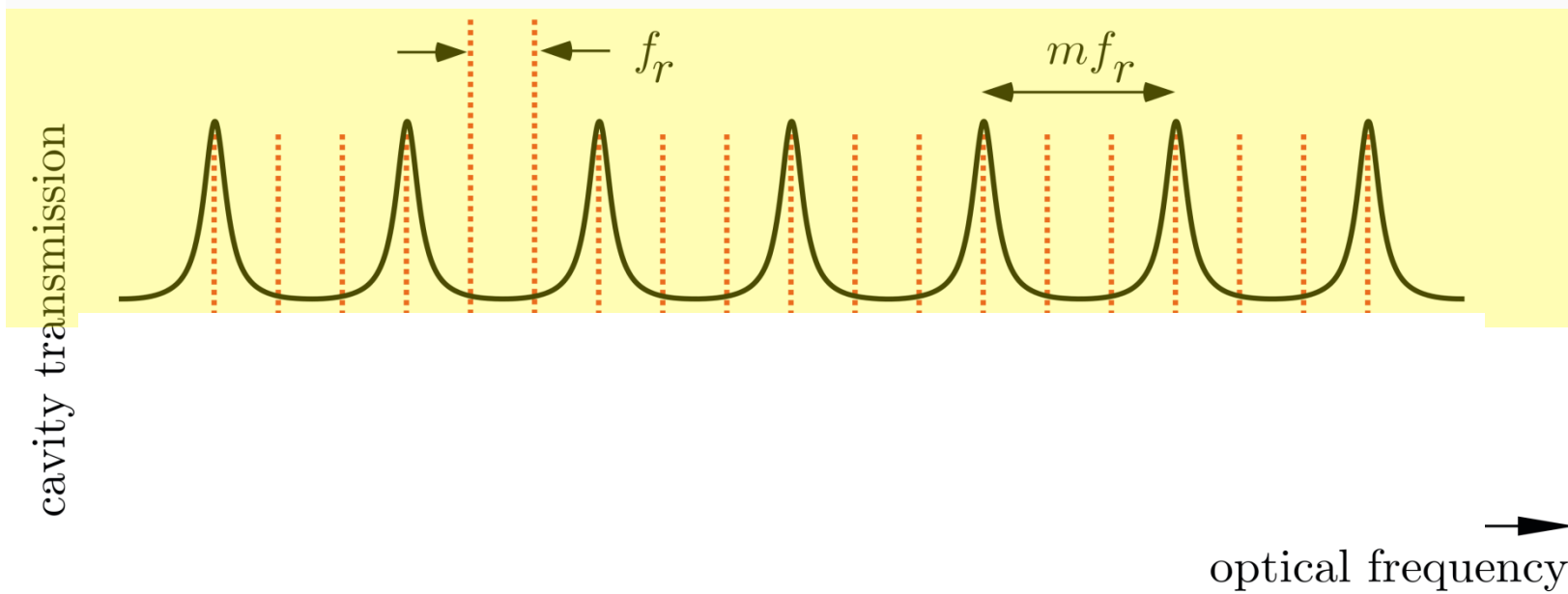
Interferential optical filtering

Filter out the unwanted modes with an external Fabry-Perot (F-P) cavity

Filtering order $m = FSR / f_r$ (160 for GIANO)

Requirements:

- High side-mode suppression ρ





Interferential optical filtering

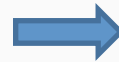
•Side-mode suppression

$$\rho = T(f_r, R, L) \quad \text{with} \quad T(f, R, L) = \frac{(1 - R)^2}{(1 - R)^2 + 4R \sin^2(2\pi fL/c)}$$

R : mirror reflectivity
 L : cavity length

Spectral shift for remaining side modes:

$$\Delta f = \frac{0 + \rho f_r}{1 + \rho} \simeq \rho f_r$$



$$\rho \simeq \frac{\Delta f}{f} \frac{f}{f_r}$$

GIANO's request:

$$\Delta f/f = v/c = 3 \times 10^{-10}$$

$$\begin{matrix} f=200\text{THz} \\ f_r=100\text{MHz} \end{matrix}$$

$$\rho = -32 \text{ dB} \rightarrow \text{Finesse} \quad F \approx \frac{\pi}{1 - R}$$

$$F \sim 3000 \quad (R = 99.9\%)$$

•Cavity-mirrors dispersion

$$FSR(f) = \frac{c}{2L + (c/\pi)\partial\phi/\partial f}$$

$\partial\phi/\partial f$: round-trip phase shift due to mirror reflections



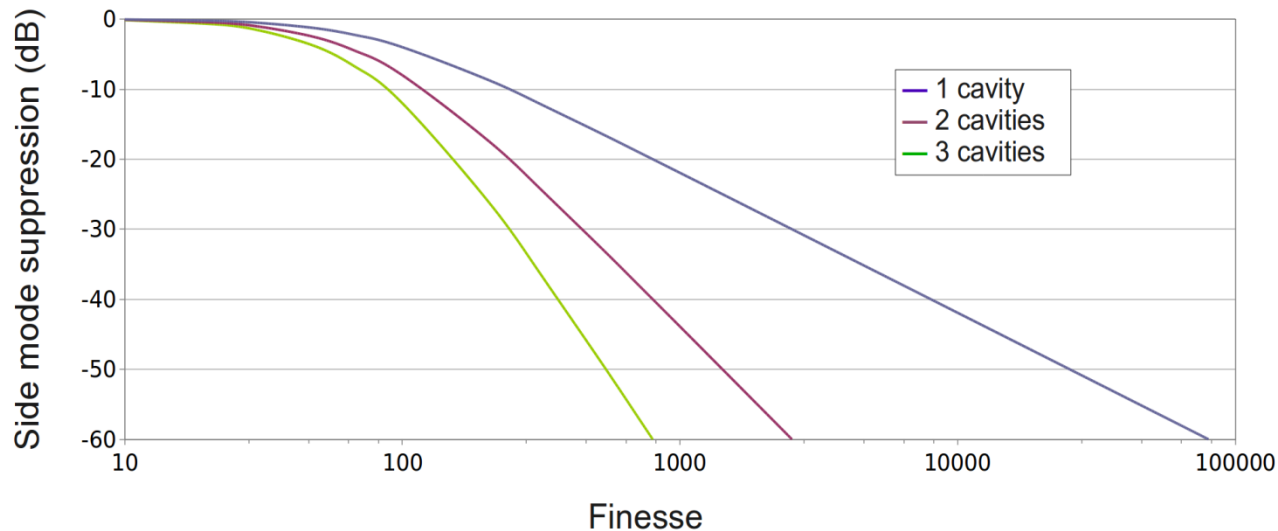
> Finesse → > dispersion

Conflicting requirements: high finesse for good side-mode suppression, low finesse to reduce mismatches.



Interferential optical filtering

Solution: more than one F-P cavity in series



Case $\rho = -32$ dB

- ◆ 1 cavity: $F = 3000$
($R = 99.9\%$)
- ◆ 2 cavities: $F = 500$
($R = 99.4\%$)
- ◆ 3 cavities: $F = 250$
($R = 98.7\%$)

Cavity-mirrors dispersion: Group Delay Dispersion (GDD)

$$GDD(f) = \frac{d}{df} \frac{1}{FSR(f)} [fs^2]$$

GIANO's request:

$FSR = 16$ GHz

$f_r = 100$ MHz

0.1% FSR change between 1-2 μ m



$GDD < 150$ fs²



Design of a filtering system

Feasibility of a 16GHz OFC calibrator in the 1-2 μm operation range with $\rho < 32\text{dB}$ and $\text{GDD} < 100\text{fs}^2$

1st approach:

2 cavities ($\text{FSR}_1 = 1.6\text{ GHz}$ and $\text{FSR}_2 = 16\text{GHz}$) in series made of **dielectric** coated mirrors ($F = 320$ and $\text{GDD} < 100\text{ fs}^2$)
in the range 1500 – 1650 nm
+
spectral broadening in a
highly non-linear fiber (HNLF).

2nd approach:

3 cavities ($\text{FSR}_1 = 1.6\text{ GHz}$ $\text{FSR}_2 = 8\text{GHz}$ and $\text{FSR}_3 = 16\text{GHz}$) in series
made of **metallic** coated mirrors ($F = 100$ and $\text{GDD} = 0\text{ fs}^2$)
in the range 1000 – 2000 nm.



Design of a filtering system

Additional constraints

- Transversal high order modes

$$f_{qmn} = \frac{c}{2L} \left[q + (n + m + 1) \frac{\arccos(\sqrt{g_1 g_2})}{\pi} \right]$$

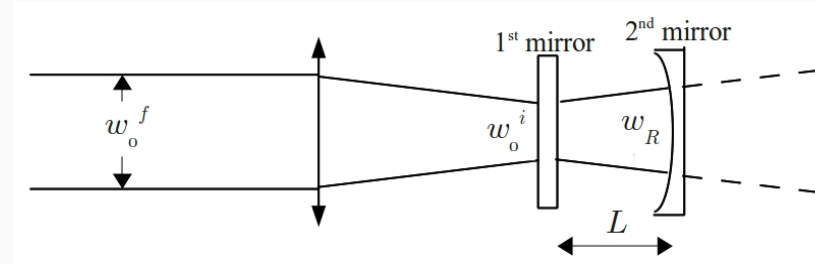


Define optical configuration of the F-P's

spot size at 1st mirror:

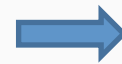
$$w_0^i = \left[(R - L) \frac{\lambda^2}{\pi^2} L \right]^{1/4}$$

hemifocal cavities ($R_2 = 100$ mm)



- Final power / comb mode

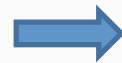
Defined by the spectrograph sensitivity



For GIANO:

total power 16 – 165 pW in the 1-2 μ m range

- Air dispersion inside the F-P's

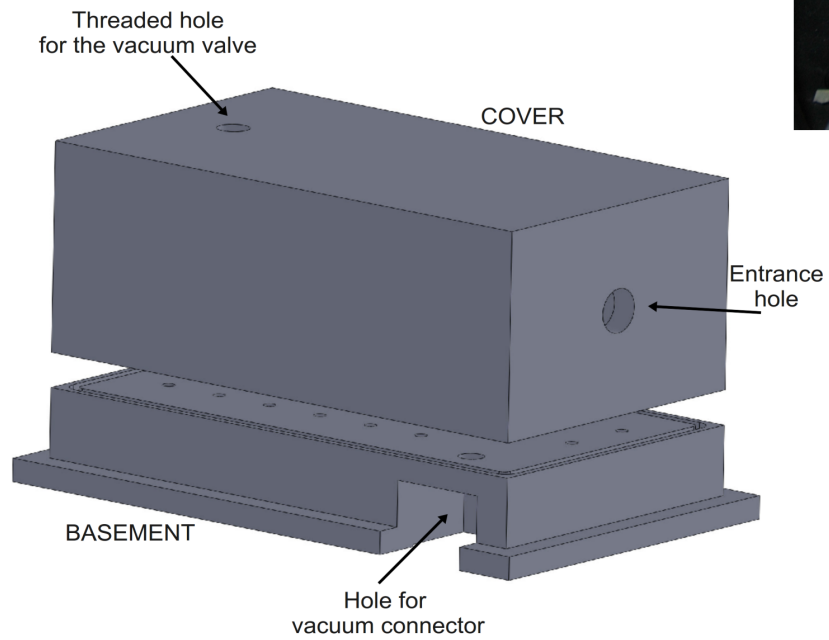
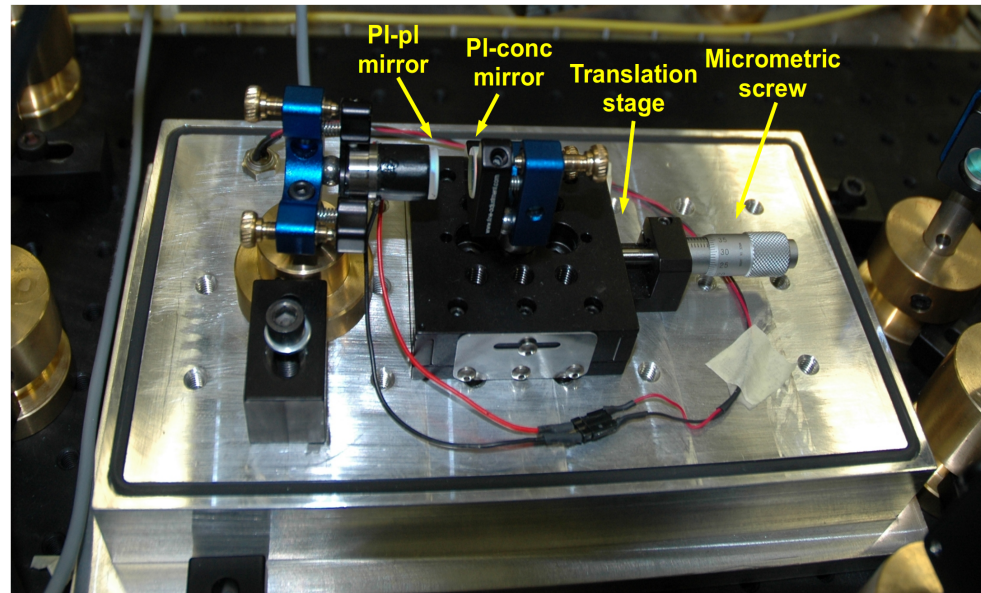


Cavities under vacuum



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F-P cavity

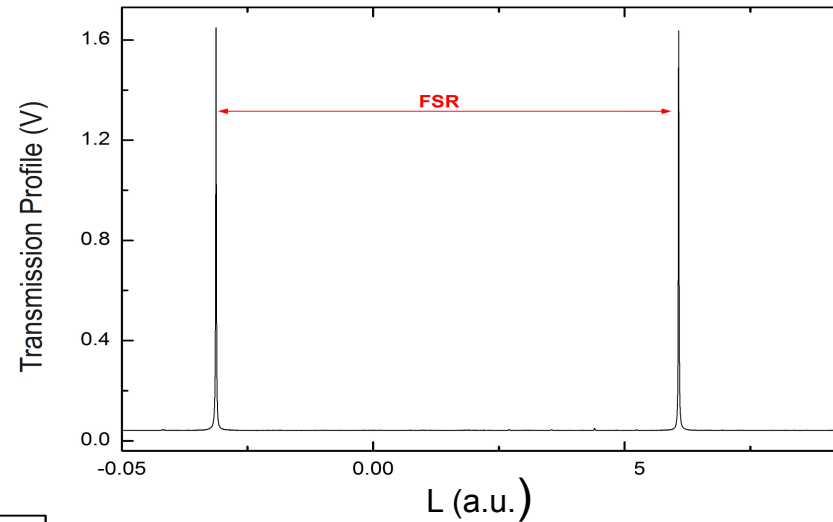
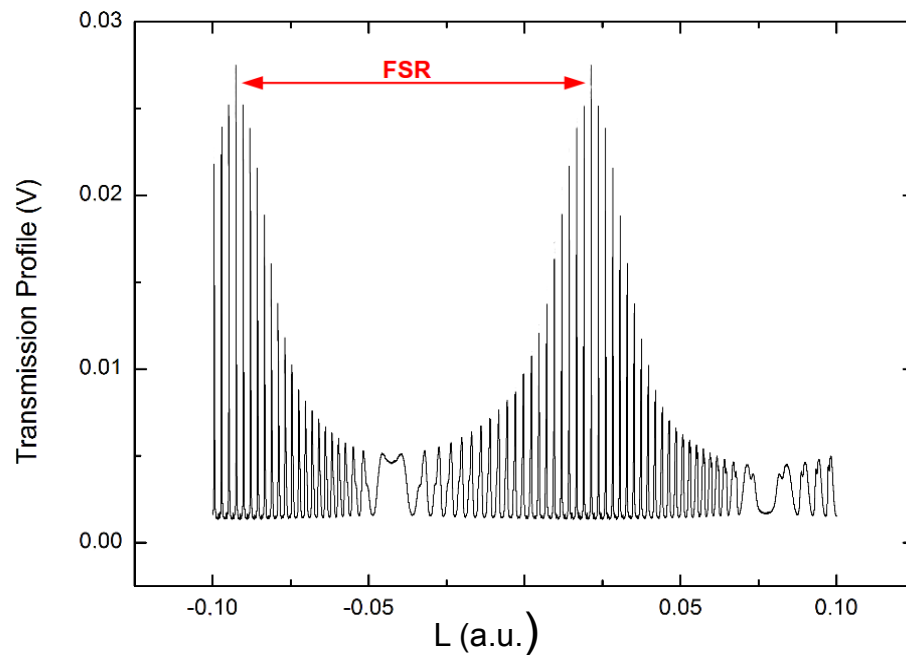




F-P cavity

Cavity alignment

Mirror alignment by using a cw laser at 1550 nm



$$\frac{c}{2L} = m f_r$$

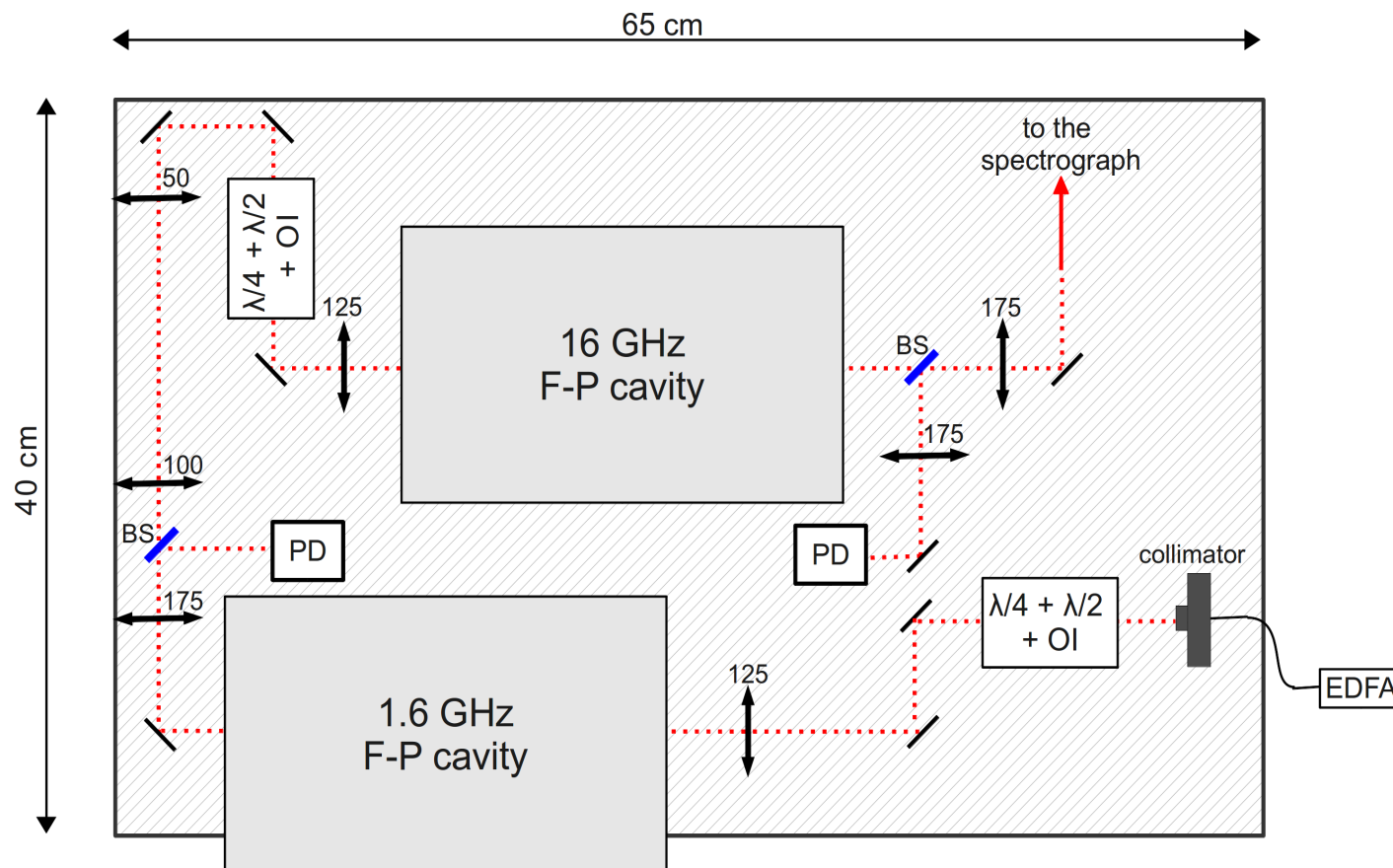
m integer only in perfect comb matching



F-P with dielectric coated mirrors

$FSR_1 = 1.6 \text{ GHz} \rightarrow \rho = -32 \text{ dB}$ with $F = 320$

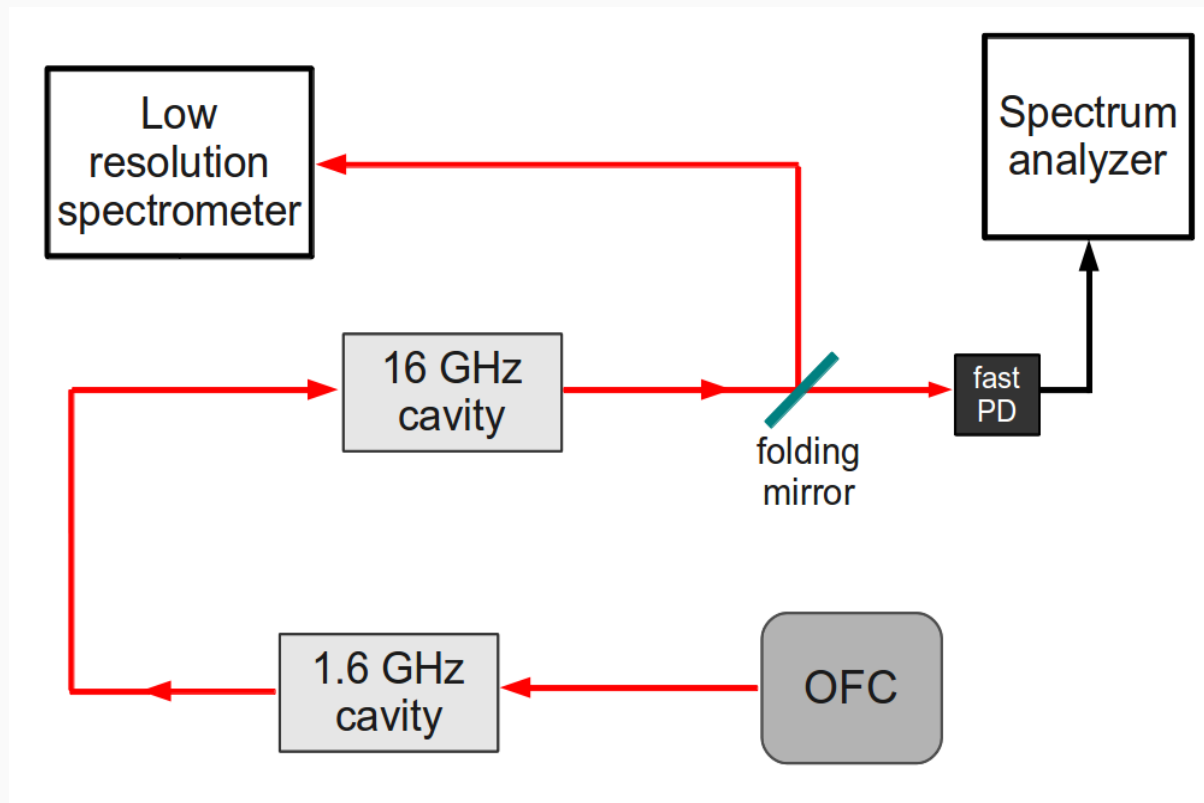
$FSR_2 = 16 \text{ GHz} \rightarrow \rho = -44 \text{ dB}$ and $\rho_{1.6\text{GHz}} = -32 \text{ dB}$ with $F = 320$





F-P with dielectric coated mirrors

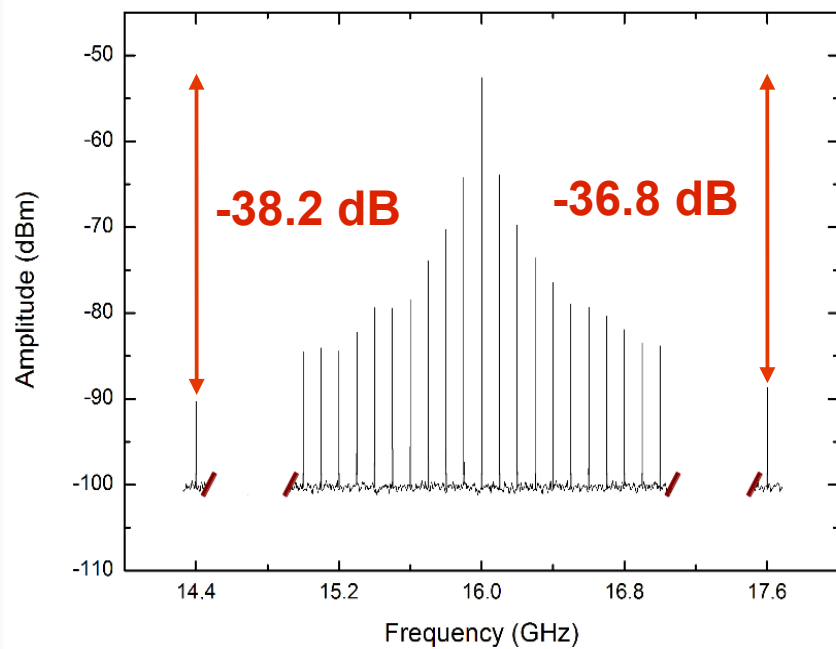
Filtering characterization



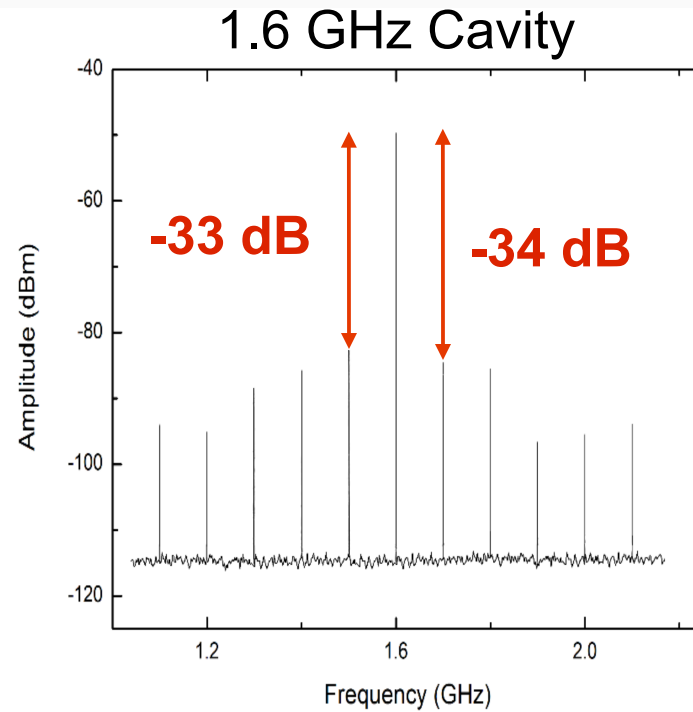


F-P with dielectric coated mirrors

The 100 MHz OFC coupled
in each cavity



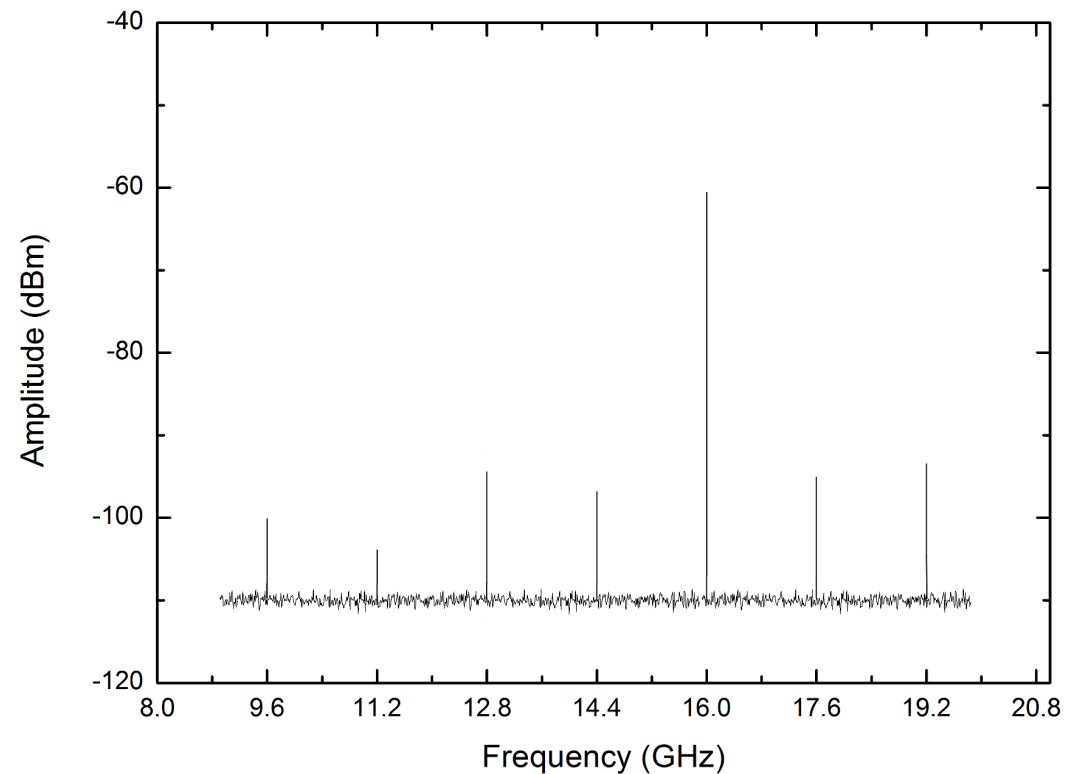
16 GHz Cavity





F-P with dielectric coated mirrors

Two F-P in series

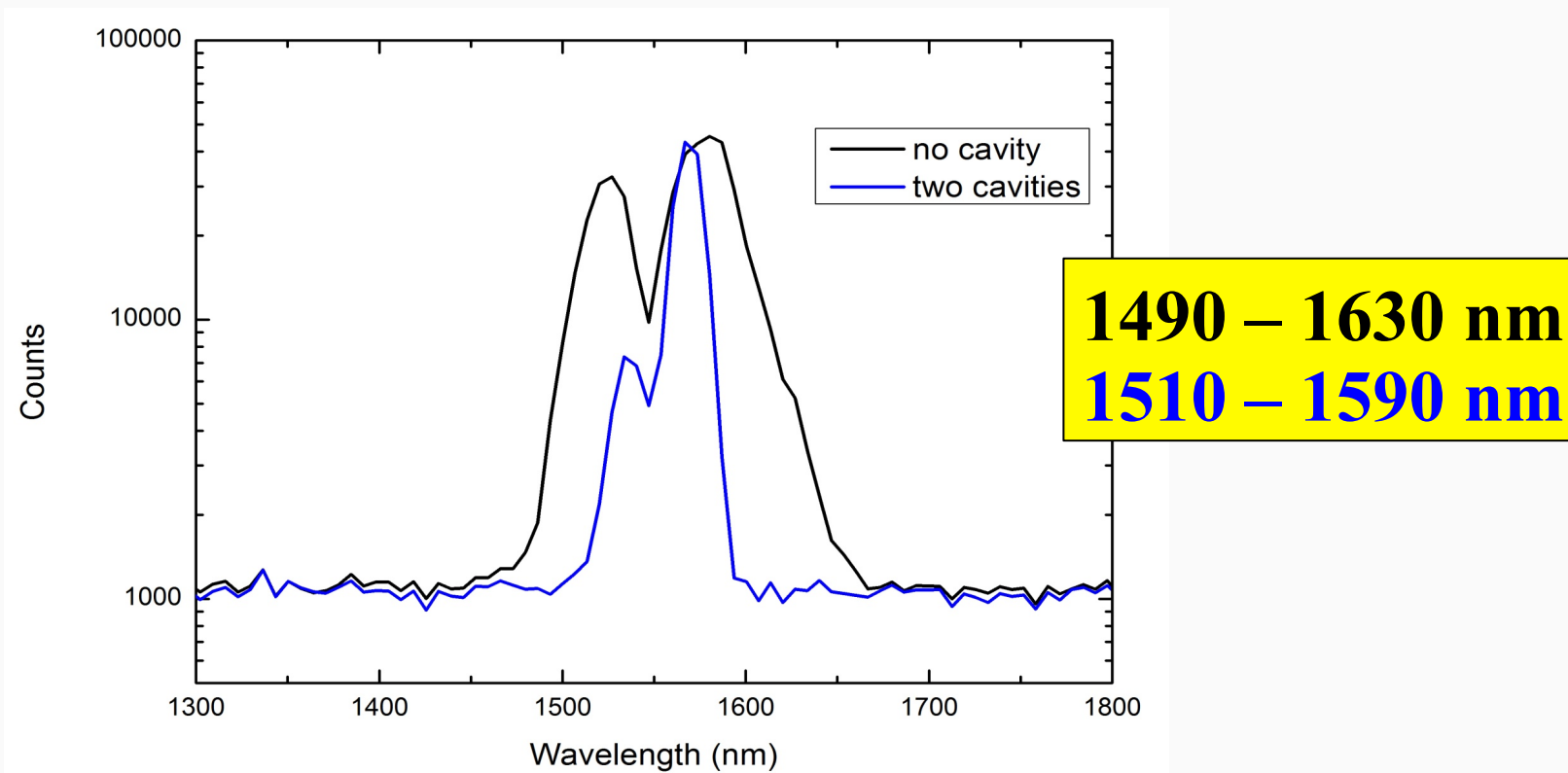


More than 35 dB suppression



F-P with dielectric coated mirrors

Spectral coverage



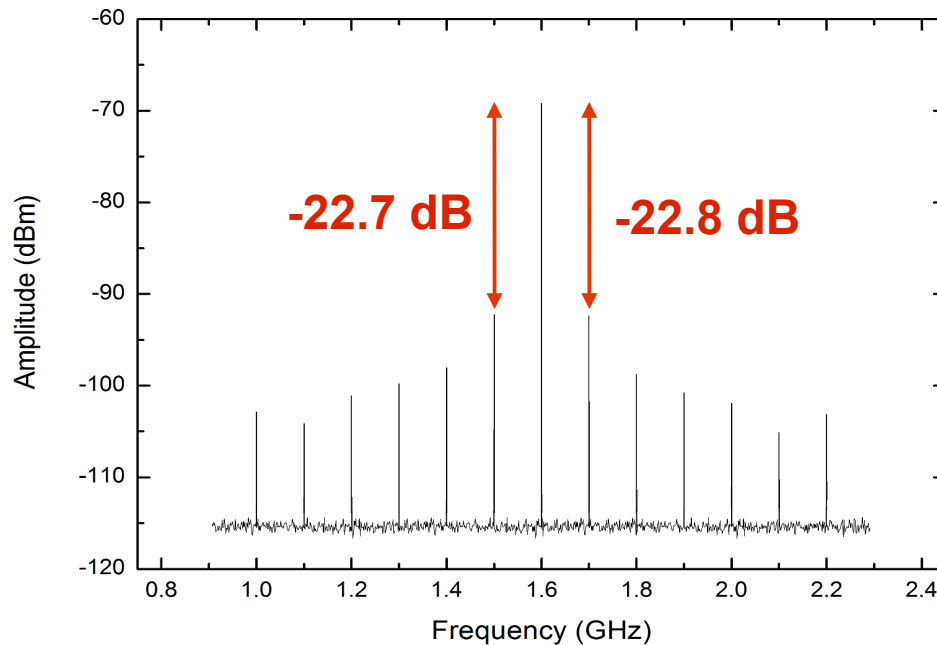
Final Power : 300 μ W with a loss factor of 1500 \rightarrow insufficient for spectral broadening



F-P with metallic coated mirrors

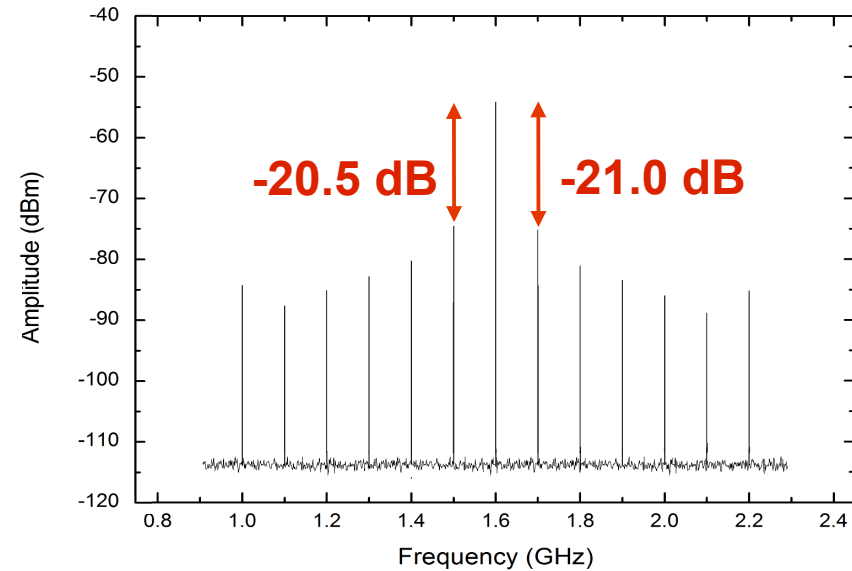
The 100 MHz OFC
coupled in 1.6 GHz Cavity

Required suppression: $\rho = -20.8$ dB



$R = 98.5\%$, $T = 0.2\%$

$R = 97.5\%$, $T = 0.4\%$



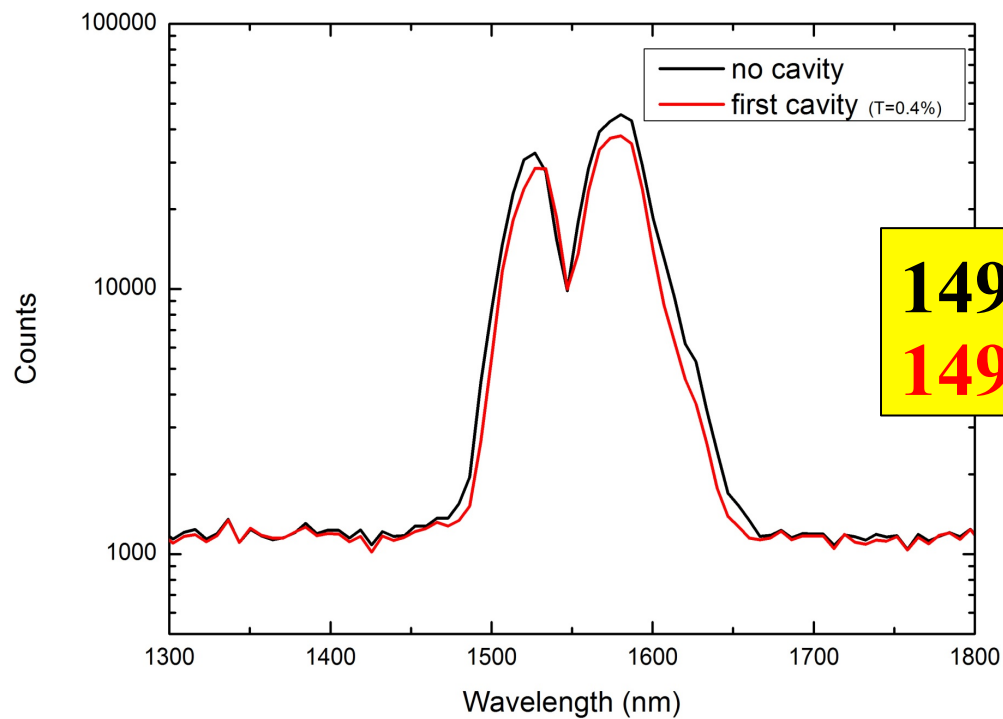
Higher suppression but 5
times higher power losses

$$R + T \neq 1 (A > T)$$



F-P with metallic coated mirrors

Spectral coverage



1490 – 1630 nm
1490 – 1630 nm

Final Power : $30\mu\text{W}$ with a loss factor of 15000



Dielectric cavities:

- ADVANTAGES:
 - ✓ high $R \rightarrow 2$ cavities
 - ✓ low power losses
- DISADVANTAGES:
 - ✓ limited spectral coverage
 $\rightarrow 1500 - 1650$ nm
 - ✓ not enough power for spectral broadening
 - ✓ worsening suppression due to further amplification

Metallic cavities:

- ADVANTAGES:
 - ✓ no dispersion
 \rightarrow octave spanning
- DISADVANTAGES:
 - ✓ low $R \rightarrow 3$ cavities
 - ✓ high power losses



...and perspectives

- Microcavity OFC
 - ✓ Directly emitting at high repetition rate
 - ◆ Difficult to control and stabilize
- EOM generated OFC:
 - ✓ Directly emitting at high repetition rate
 - ◆ Limited spectral coverage
 - ◆ Difficult to produce rep. rate high than 10 GHz
 - ◆ Optical reference to be stabilized

Grazie della attenzione



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15 febbraio 2013

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